Graduate Aptitude Test in Engineering 2017

Question Paper Name: Engineering Sciences 12th Feb 2017
Subject Name: Engineering Sciences
Duration: 180
Total Marks: 100

Organizing Institute:

Indian Institute of Technology Roorkee

Engineering Mathematics (XE-A) (Compulsory)

Question Number : 1 **Correct : 1 Wrong : 0**

If

$$\int_0^{\frac{\pi}{\alpha}} \int_x^{\frac{\pi}{\alpha}} \frac{\sin y}{y}\, dy\, dx = \frac{1}{2}$$

for some $\alpha \geq 1$, then the value of α is _____.

Question Number : 2 **Correct : 1 Wrong : -0.33**

Three fair dice are rolled simultaneously. The probability of getting a sum of 5 is

(A) $\frac{1}{108}$ (B) $\frac{1}{72}$ (C) $\frac{1}{54}$ (D) $\frac{1}{36}$

Question Number : 3 **Correct : 1 Wrong : 0**

Suppose α, β, γ and δ are constants such that

$$p(x) = \delta + \gamma\,(x+1) + \beta\, x(x+1) + \alpha\, x\,(x+1)(x-1)$$

is the interpolating polynomial for the data $(-1,-3), (0,1), (1,-1)$, and $(2,-3)$. Then the value of $\gamma - \beta$ is _____.

Question Number : 4 **Correct : 1 Wrong : 0**

Consider the ordinary differential equation

$$y'' + \alpha\, y' + \beta\, y = 0,$$

where α and β are constants. If $y(x) = x\, e^x$ is a solution of the above equation, then the value of $\beta - \alpha$ is _____.

Question Number : 5 **Correct : 1 Wrong : -0.33**

Consider the system of linear equations

$$\begin{aligned} 2x_2 + x_3 &= 0, \\ -2x_1 - x_3 &= 0, \\ -x_1 + x_2 &= 1. \end{aligned}$$

The above system has

(A) a unique solution
(B) infinite number of solutions
(C) no solution
(D) only two distinct solutions

Question Number : 6 **Correct : 1 Wrong : 0**

Let C be a simple smooth closed curve enclosing the region R in the xy-plane. Let C be oriented counterclockwise. If the value of the integral

$$\oint_C (y + e^{x^2})dx + (3x + \cos y)\, dy$$

is 16, then the area of R is _____.

Question Number : 7 **Correct : 1 Wrong : -0.33**

Consider the ordinary differential equation

$$x^2y'' + xy' - y = x, \quad x > 0.$$

In terms of arbitrary constants c_1 and c_2, the general solution of the above equation is

(A) $y(x) = c_1x + c_2x^{-1} + x^3$

(B) $y(x) = c_1x^2 + c_2x^{-1} + \frac{1}{2}x$

(C) $y(x) = c_1x + c_2x^{-1} + \frac{1}{2}x \ln x$

(D) $y(x) = c_1x + c_2 + x^{-1}$

Question Number : 8 **Correct : 2 Wrong : -0.66**

Let $f: \mathbb{R} \to \mathbb{R}$ and $g: \mathbb{R} \to \mathbb{R}$ be defined by

$$f(x) = \begin{cases} x\,(\sin x)\cos\frac{1}{x}, & x \neq 0 \\ 0, & x = 0 \end{cases} \quad \text{and} \quad g(x) = \begin{cases} x\cos\frac{1}{x}, & x \neq 0 \\ 0, & x = 0, \end{cases}$$

where $\mathbb{R}$ denotes the set of real numbers. Then, at $x = 0$,

(A) f is differentiable but g is NOT differentiable

(B) f is NOT differentiable but g is differentiable

(C) both f and g are differentiable

(D) neither f nor g is differentiable

Question Number : 9 **Correct : 2 Wrong : 0**

If $u(x,t) = g(t)\sin x$ is the solution of the wave equation

$$u_{tt} = u_{xx}, \qquad t > 0, \qquad 0 < x < \pi,$$

with the initial conditions

$$u(x,0) = 2\sin x, \qquad u_t(x,0) = 0, \qquad 0 \le x \le \pi,$$

and the boundary conditions

$$u(0,t) = u(\pi,t) = 0, \qquad t \ge 0,$$

then the value of $g(\frac{\pi}{3})$ is _____.

Question Number : 10 **Correct : 2 Wrong : 0**

Let

$$I = \int_0^1 \frac{1}{1+t}\,dt + \frac{\pi i}{2}\int_0^1 \frac{e^{\frac{i\pi t}{2}}}{1+e^{\frac{i\pi t}{2}}}\,dt - i\int_0^1 \frac{1}{1+it}\,dt,$$

where t is a real variable and $i = \sqrt{-1}$. The value of I is _____.

Question Number : 11 **Correct : 2 Wrong : -0.66**

Let

$$a_k = 2^{-k}\,k^4\,\sin k \qquad \text{and} \qquad b_k = 2^{-k^2}\,k\,\sin^2 k$$

for $k = 1,2,\ldots$. Then

(A) $\sum_{k=1}^{\infty} a_k$ converges but $\sum_{k=1}^{\infty} b_k$ does NOT converge
(B) $\sum_{k=1}^{\infty} a_k$ does NOT converge but $\sum_{k=1}^{\infty} b_k$ converges
(C) both $\sum_{k=1}^{\infty} a_k$ and $\sum_{k=1}^{\infty} b_k$ converge
(D) neither $\sum_{k=1}^{\infty} a_k$ nor $\sum_{k=1}^{\infty} b_k$ converges

General Aptitude

Question Number : 166 **Correct : 1 Wrong : -0.33**

The event would have been successful if you _____able to come.

(A) are (B) had been (C) have been (D) would have been

Question Number : 167 **Correct : 1 Wrong : -0.33**

There was no doubt that their work was thorough.

Which of the words below is closest in meaning to the underlined word above?

(A) pretty (B) complete (C) sloppy (D) haphazard

Question Number : 168 Correct : 1 Wrong : -0.33

Four cards lie on a table. Each card has a number printed on one side and a colour on the other. The faces visible on the cards are 2, 3, red, and blue.

Proposition: If a card has an even value on one side, then its opposite face is red.

The cards which MUST be turned over to verify the above proposition are

(A) 2, red (B) 2, 3, red (C) 2, blue (D) 2, red, blue

Question Number : 169 Correct : 1 Wrong : -0.33

What is the value of x when $81 \times \left(\frac{16}{25}\right)^{x+2} \div \left(\frac{3}{5}\right)^{2x+4} = 144$?

(A) 1 (B) -1 (C) -2 (D) Cannot be determined

Question Number : 170 Correct : 1 Wrong : -0.33

Two dice are thrown simultaneously. The probability that the product of the numbers appearing on the top faces of the dice is a perfect square is

(A) 1/9 (B) 2/9 (C) 1/3 (D) 4/9

Question Number : 171 Correct : 2 Wrong : -0.66

Bhaichung was observing the pattern of people entering and leaving a car service centre. There was a single window where customers were being served. He saw that people inevitably came out of the centre in the order that they went in. However, the time they spent inside seemed to vary a lot: some people came out in a matter of minutes while for others it took much longer.

From this, what can one conclude?

(A) The centre operates on a first-come-first-served basis, but with variable service times, depending on specific customer needs.
(B) Customers were served in an arbitrary order, since they took varying amounts of time for service completion in the centre.
(C) Since some people came out within a few minutes of entering the centre, the system is likely to operate on a last-come-first-served basis.
(D) Entering the centre early ensured that one would have shorter service times and most people attempted to do this.

Question Number : 172 **Correct : 2 Wrong : -0.66**

A map shows the elevations of Darjeeling, Gangtok, Kalimpong, Pelling, and Siliguri. Kalimpong is at a lower elevation than Gangtok. Pelling is at a lower elevation than Gangtok. Pelling is at a higher elevation than Siliguri. Darjeeling is at a higher elevation than Gangtok.

Which of the following statements can be inferred from the paragraph above?

i. Pelling is at a higher elevation than Kalimpong
ii. Kalimpong is at a lower elevation than Darjeeling
iii. Kalimpong is at a higher elevation than Siliguri
iv. Siliguri is at a lower elevation than Gangtok

(A) Only ii (B) Only ii and iii (C) Only ii and iv (D) Only iii and iv

Question Number : 173 **Correct : 2 Wrong : -0.66**

P, Q, R, S, T and U are seated around a circular table. R is seated two places to the right of Q. P is seated three places to the left of R. S is seated opposite U. If P and U now switch seats, which of the following must necessarily be true?

(A) P is immediately to the right of R
(B) T is immediately to the left of P
(C) T is immediately to the left of P or P is immediately to the right of Q
(D) U is immediately to the right of R or P is immediately to the left of T

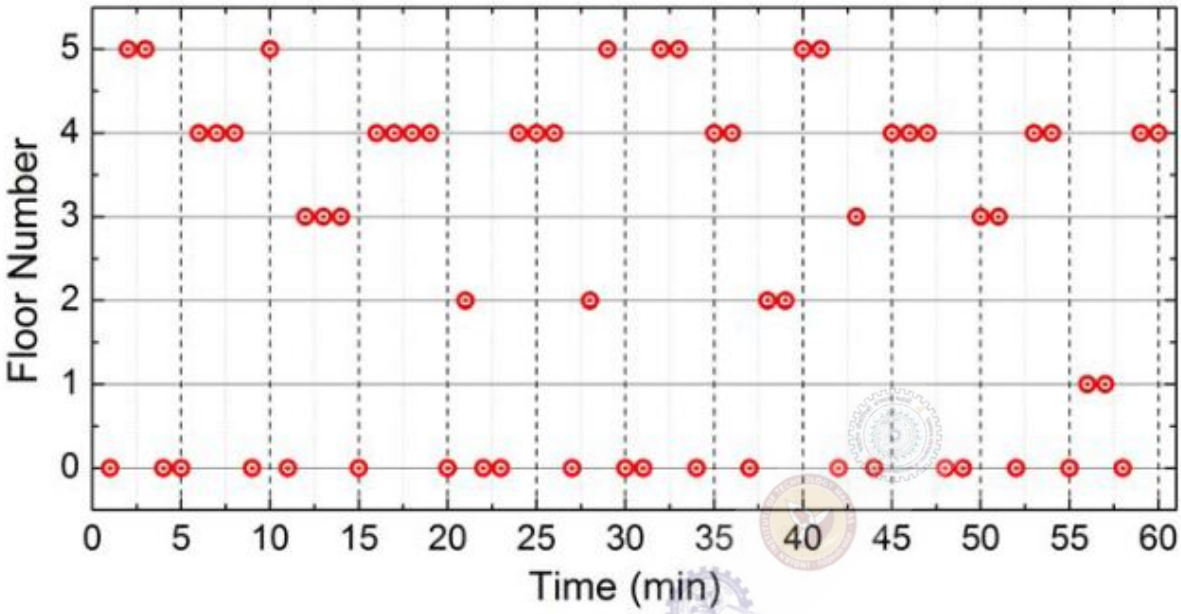
Question Number : 174 **Correct : 2 Wrong : -0.66**

Budhan covers a distance of 19 km in 2 hours by cycling one fourth of the time and walking the rest. The next day he cycles (at the same speed as before) for half the time and walks the rest (at the same speed as before) and covers 26 km in 2 hours. The speed in km/h at which Budhan walks is

(A) 1 (B) 4 (C) 5 (D) 6

Question Number : 175 **Correct : 2 Wrong : -0.66**

The points in the graph below represent the halts of a lift for durations of 1 minute, over a period of 1 hour.



Which of the following statements are correct?

i. The elevator never moves directly from any non-ground floor to another non-ground floor over the one hour period

ii. The elevator stays on the fourth floor for the longest duration over the one hour period

(A)) Only i (B) Only ii (C) Both i and ii (D) Neither i nor ii

Q. No.	Type	Section	Key	Marks
1	NAT	XE-A	2.98 to 3.02	1
2	MCQ	XE-A	D	1
3	NAT	XE-A	6.98 to 7.02	1
4	NAT	XE-A	2.98 to 3.02	1
5	MCQ	XE-A	C	1
6	NAT	XE-A	7.98 to 8.02	1
7	MCQ	XE-A	C	1
8	MCQ	XE-A	A	2
9	NAT	XE-A	0.98 to 1.02	2
10	NAT	XE-A	-0.02 to 0.02	2
11	MCQ	XE-A	C	2
12	MCQ	XE-B	B	1
13	MCQ	XE-B	B	1
14	MCQ	XE-B	C	1
15	MCQ	XE-B	A	1
16	MCQ	XE-B	D	1
17	MCQ	XE-B	D	1
18	MCQ	XE-B	A	1
19	NAT	XE-B	22.6 to 22.6	1
20	MCQ	XE-B	A	1
21	NAT	XE-B	72.5 to 75.0	2
22	NAT	XE-B	62 to 66	2
23	MCQ	XE-B	D	2
24	MCQ	XE-B	C	2
25	NAT	XE-B	0.66 to 0.67	2
26	NAT	XE-B	6005 to 6005	2
27	NAT	XE-B	0.05 to 0.06	2
28	MCQ	XE-B	D	2
29	NAT	XE-B	1.3 to 1.4	2
30	NAT	XE-B	28.9 to 31.4	2
31	NAT	XE-B	0.21 to 0.22	2
32	NAT	XE-B	7.0 to 7.2	2
33	MCQ	XE-B	B	2
34	MCQ	XE-C	B	1
35	MCQ	XE-C	D	1
36	MCQ	XE-C	C	1

37	MCQ	XE-C	B	1
38	MCQ	XE-C	A	1
39	MCQ	XE-C	C	1
40	MCQ	XE-C	D	1
41	MCQ	XE-C	B	1
42	MCQ	XE-C	D	1
43	NAT	XE-C	0.990 to 1.010	2
44	NAT	XE-C	53.0 to 53.2	2
45	MCQ	XE-C	A	2
46	MCQ	XE-C	A	2
47	NAT	XE-C	7.5 to 7.7	2
48	NAT	XE-C	37.5 to 38.5	2
49	MCQ	XE-C	B	2
50	NAT	XE-C	7.50 to 7.80	2
51	NAT	XE-C	172 to 174	2
52	MCQ	XE-C	D	2
53	NAT	XE-C	1.35 to 1.37	2
54	MCQ	XE-C	C	2
55	MCQ	XE-C	A	2
56	NAT	XE-D	69 to 73	1
57	MCQ	XE-D	B	1
58	MCQ	XE-D	C	1
59	MCQ	XE-D	C	1
60	MCQ	XE-D	A	1
61	MCQ	XE-D	B	1
62	MCQ	XE-D	A	1
63	NAT	XE-D	0.26 to 0.28	1
64	MCQ	XE-D	A	1
65	MCQ	XE-D	D	2
66	NAT	XE-D	134 to 136	2
67	NAT	XE-D	0.55 to 0.65	2
68	NAT	XE-D	1785 to 1792	2
69	NAT	XE-D	0.45 to 0.50	2
70	NAT	XE-D	32 to 35	2
71	NAT	XE-D	10 to 10	2
72	NAT	XE-D	02 to 02	2
73	MCQ	XE-D	A	2

74	NAT	XE-D	17 to 18	2
75	MCQ	XE-D	C	2
76	MCQ	XE-D	B	2
77	MCQ	XE-D	B	2
78	MCQ	XE-E	B	1
79	MCQ	XE-E	C	1
80	MCQ	XE-E	C	1
81	NAT	XE-E	0.17 to 0.18	1
82	MCQ	XE-E	B	1
83	MCQ	XE-E	D	1
84	MCQ	XE-E	A	1
85	MCQ	XE-E	B	1
86	NAT	XE-E	499 to 501	1
87	NAT	XE-E	53 to 55	2
88	MCQ	XE-E	D	2
89	NAT	XE-E	0.026 to 0.030	2
90	NAT	XE-E	73.5 to 73.8	2
91	NAT	XE-E	2.2 to 2.2	2
92	NAT	XE-E	0.140 to 0.150	2
93	MCQ	XE-E	C	2
94	MCQ	XE-E	A	2
95	MCQ	XE-E	A	2
96	NAT	XE-E	2225 to 2230	2
97	NAT	XE-E	0.76 to 0.82	2
98	NAT	XE-E	29.0 to 30.0	2
99	NAT	XE-E	60.5 to 61.5	2
100	MCQ	XE-F	D	1
101	MCQ	XE-F	B	1
102	MCQ	XE-F	A	1
103	MCQ	XE-F	C	1
104	MCQ	XE-F	A	1
105	MCQ	XE-F	D	1
106	MCQ	XE-F	C	1
107	MCQ	XE-F	D	1
108	MCQ	XE-F	A	1
109	MCQ	XE-F	B	2
110	MCQ	XE-F	C	2

111	NAT	XE-F	55.95 to 56.55	2
112	NAT	XE-F	1.14 to 1.24	2
113	MCQ	XE-F	C	2
114	NAT	XE-F	410 to 418	2
115	MCQ	XE-F	B	2
116	MCQ	XE-F	A	2
117	NAT	XE-F	98.5 to 99.5	2
118	NAT	XE-F	41.00 to 42.20	2
119	MCQ	XE-F	D	2
120	NAT	XE-F	-67.3 to -66.3	2
121	MCQ	XE-F	B	2
122	MCQ	XE-G	B	1
123	MCQ	XE-G	B	1
124	MCQ	XE-G	D	1
125	MCQ	XE-G	B	1
126	NAT	XE-G	1000 to 1000	1
127	MCQ	XE-G	A	1
128	NAT	XE-G	2078 to 2086	1
129	NAT	XE-G	0.80 to 0.90	1
130	MCQ	XE-G	A	1
131	MCQ	XE-G	C	2
132	MCQ	XE-G	B	2
133	MCQ	XE-G	D	2
134	NAT	XE-G	25550 to 25650	2
135	MCQ	XE-G	D	2
136	NAT	XE-G	53.30 to 55.25	2
137	NAT	XE-G	64.0 to 64.0	2
138	NAT	XE-G	0.14 to 0.18	2
139	MCQ	XE-G	D	2
140	NAT	XE-G	6.80 to 7.20	2
141	NAT	XE-G	10.80 to 11.20	2
142	NAT	XE-G	9000 to 9000	2
143	NAT	XE-G	0.30 to 0.40	2
144	MCQ	XE-H	B	1
145	MCQ	XE-H	C	1
146	NAT	XE-H	98.9 to 100.5	1
147	MCQ	XE-H	D	1

148	MCQ	XE-H	B	1
149	MCQ	XE-H	D	1
150	MCQ	XE-H	C	1
151	MCQ	XE-H	A	1
152	MCQ	XE-H	B	1
153	NAT	XE-H	22.05 to 22.15	2
154	NAT	XE-H	0.59 to 0.61	2
155	NAT	XE-H	286.55 to 287.55	2
156	MCQ	XE-H	C	2
157	NAT	XE-H	-4.10 to -3.90	2
158	NAT	XE-H	0.42 to 0.46	2
159	NAT	XE-H	51 to 52	2
160	MCQ	XE-H	B	2
161	MCQ	XE-H	A	2
162	NAT	XE-H	199 to 205	2
163	MCQ	XE-H	D	2
164	MCQ	XE-H	C	2
165	MCQ	XE-H	B	2
166	MCQ	GA	B	1
167	MCQ	GA	B	1
168	MCQ	GA	C	1
169	MCQ	GA	B	1
170	MCQ	GA	B	1
171	MCQ	GA	A	2
172	MCQ	GA	C	2
173	MCQ	GA	C	2
174	MCQ	GA	D	2
175	MCQ	GA	D	2