

NCERT SOLUTIONS

CLASS - 10th

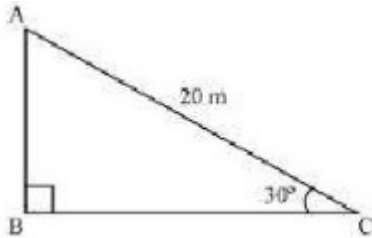


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Class : 10th
Subject : Maths
Chapter : 9
Chapter Name : Some Applications of Trigonometry

Exercise 9.1

Q1 A circus artist is climbing a 20 m long rope, which is tightly stretched and tied from the top of a vertical pole to the ground. Find the height of the pole, if the angle made by the rope with the ground level is 30° .



Answer.

It can be observed from the figure that AB is the pole. In $\triangle ABC$,

$$\frac{AB}{AC} = \sin 30^\circ$$

$$\frac{AB}{20} = \frac{1}{2}$$

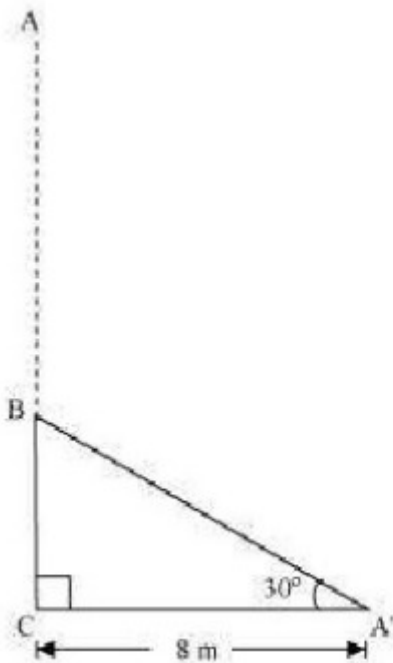
$$AB = \frac{20}{2} = 10$$

Therefore, the height of the pole is 10m .

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Q2 A tree breaks due to storm and the broken part bends so that the top of the tree touches the ground making an angle 30° with it. The distance between the foot of the tree to the point where the top touches the ground is 8 m. Find the height of the tree.

Answer.



Let AC was the original tree. Due to storm, it was broken into parts. The broken part A'B is making 30° with the ground.

In $\triangle A'BC$

$$\frac{BC}{A'C} = \tan 30^\circ$$

$$\frac{BC}{8} = \frac{1}{\sqrt{3}}$$

$$BC = \left(\frac{8}{\sqrt{3}}\right) \text{ m}$$

$$\frac{A'C}{A'B} = \cos 30^\circ$$

$$\frac{8}{A'B} = \frac{\sqrt{3}}{2}$$

$$A'B = \left(\frac{16}{\sqrt{3}}\right) \text{ m}$$

$$\text{Height of tree} = A'B + BC$$

$$= \left(\frac{16}{\sqrt{3}} + \frac{8}{\sqrt{3}}\right) \text{ m} = \frac{24}{\sqrt{3}} \text{ m}$$

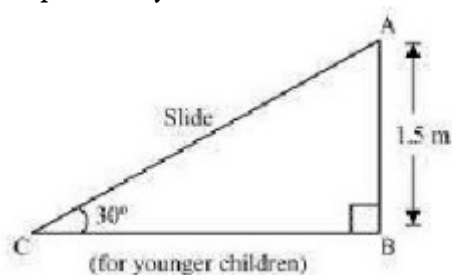
$$= 8\sqrt{3} \text{ m}$$

Hence, the height of the tree is $8\sqrt{3} \text{ m}$.

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Q3 A contractor plans to install two slides for the children to play in a park. For the children below the age of 5 years, she prefers to have a slide whose top is at a height of 1.5 m, and is inclined at an angle of 30° to the ground, where as for the elder children she wants to have a steep side at a height of 3 m, and inclined at an angle of 60° to the ground. What should be the length of the slide in each case?

Answer. It can be observed that AC and PR are the slides for younger and elder children respectively.

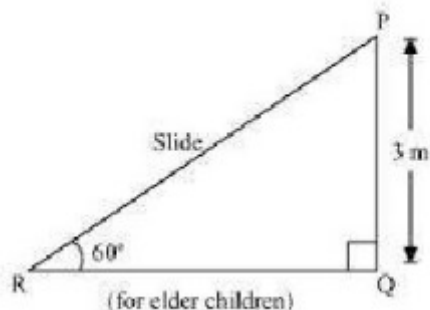


In $\triangle ABC$,

$$\frac{AB}{AC} = \sin 30^\circ$$

$$\frac{1.5}{AC} = \frac{1}{2}$$

$$AC = 3\text{m}$$



In $\triangle PQR$,

$$\frac{PQ}{PR} = \sin 60^\circ$$

$$\frac{3}{PR} = \frac{\sqrt{3}}{2}$$

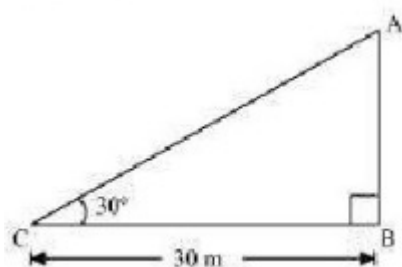
$$PR = \frac{6}{\sqrt{3}} = 2\sqrt{3}\text{m}$$

Therefore, the length of these slides are 3 m and $2\sqrt{3}\text{m}$.

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Q4 The angle of elevation of the top of a tower from a point on the ground, which is 30 m away from the foot of the tower is 30° . Find the height of the tower.

Answer.



Let AB be the tower and the angle of elevation from point C(on ground) is 30° .

In $\triangle ABC$,

$$\frac{AB}{BC} = \tan 30^\circ$$

$$\frac{AB}{30} = \frac{1}{\sqrt{3}}$$

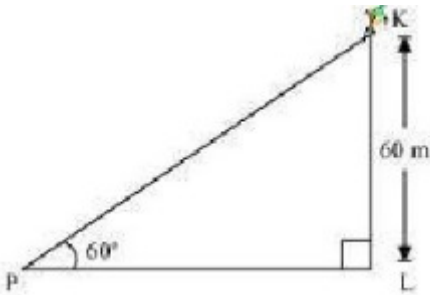
$$AB = \frac{30}{\sqrt{3}} = 10\sqrt{3}\text{m}$$

Therefore, the height of the tower is $10\sqrt{3}\text{m}$.

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Q5 A kite is flying at a height of 60 m above the ground. The string attached to the kite is temporarily tied to a point on the ground. The inclination of the string with the ground is 60° . Find the length of the string, assuming that there is no slack in the string.

Answer.



Let K be the kite and the string is tied to point P on the ground.

In $\triangle KLP$,

$$\frac{KL}{KP} = \sin 60^\circ$$

$$\frac{60}{KP} = \frac{\sqrt{3}}{2}$$

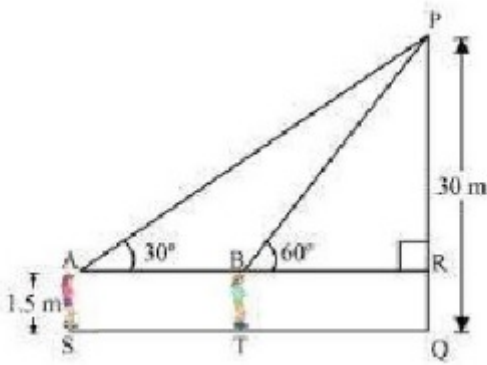
$$KP = \frac{120}{\sqrt{3}} = 40\sqrt{3}\text{m}$$

Hence, the length of the string is $40\sqrt{3}\text{m}$.

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Q6 A 1.5 m tall boy is standing at some distance from a 30 m tall building. The angle of elevation from his eyes to the top of the building increases from 30° to 60° as he walks towards the building. Find the distance he walked towards the building.

Answer.



Let the boy was standing at point S initially. He walked towards the building and reached at point T.

It can be observed that

$$PR = PQ - RQ$$

$$= (30 - 1.5)\text{m} = 28.5\text{m} = \frac{57}{2}\text{m}$$

In $\triangle PAR$,

$$\frac{PR}{AR} = \tan 30^\circ$$

$$\frac{\frac{57}{2}}{AR} = \frac{1}{\sqrt{3}}$$

$$AR = \left(\frac{57}{2}\sqrt{3}\right)\text{m}$$

In $\triangle PRB$,

$$\frac{PR}{BR} = \tan 60^\circ$$

$$\frac{\frac{57}{2}}{BR} = \sqrt{3}$$

$$BR = \frac{57}{2\sqrt{3}} = \left(\frac{19\sqrt{3}}{2}\right)\text{m}$$

$$ST = AB$$

$$= AR - BR = \left(\frac{57\sqrt{3}}{2} - \frac{19\sqrt{3}}{2}\right)\text{m}$$

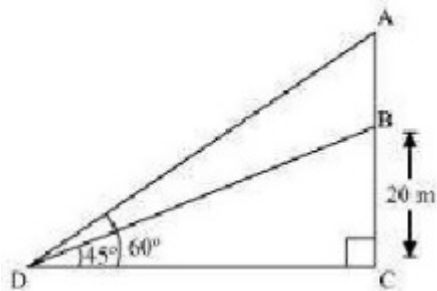
$$= \left(\frac{38\sqrt{3}}{2}\right)\text{m} = 19\sqrt{3}\text{m}$$

Hence, he walked $19\sqrt{3}$ m towards the building.

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Q7 From a point on the ground, the angles of elevation of the bottom and the top of a transmission tower fixed at the top of a 20 m high building are 45° and 60° respectively. Find the height of the tower.

Answer.



Let BC be the building, AB be the transmission tower, and D be the point on the ground from where the elevation angles are to be measured.

In $\triangle BCD$,

$$\frac{BC}{CD} = \tan 45^\circ$$

$$\frac{20}{CD} = 1$$

$$CD = 20\text{m}$$

In $\triangle ACD$

$$\frac{AC}{CD} = \tan 60^\circ$$

$$\frac{AB+BC}{CD} = \sqrt{3}$$

$$\frac{AB+20}{20} = \sqrt{3}$$

$$AB = (20\sqrt{3} - 20)\text{m}$$

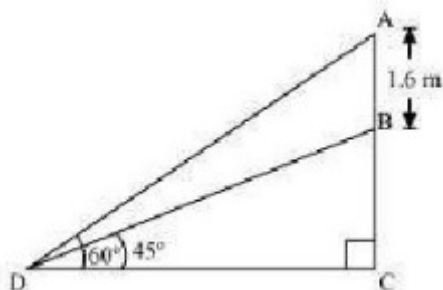
$$= 20(\sqrt{3} - 1)\text{m}$$

Therefore, the height of the transmission tower is $20(\sqrt{3} - 1)\text{m}$.

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Q8 A statue, 1.6 m tall, stands on a top of pedestal, from a point on the ground, the angle of elevation of the top of statue is 60° and from the same point the angle of elevation of the top of the pedestal is 45° . Find the height of the pedestal.

Answer.



Let AB be the statue, BC be the pedestal, and D be the point on the ground from where the elevation angles are to be measured.

In $\triangle BCD$,

$$\frac{BC}{CD} = \tan 45^\circ$$

$$\frac{BC}{CD} = 1$$

$$BC = CD$$

In $\triangle ACD$,

$$\frac{AB+BC}{CD} = \tan 60^\circ$$

$$\frac{AB+BC}{BC} = \sqrt{3}$$

$$1.6 + BC = BC\sqrt{3}$$

$$BC(\sqrt{3} - 1) = 1.6$$

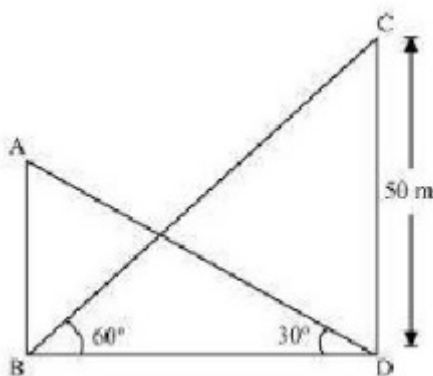
$$\begin{aligned} BC &= \frac{(1.6)(\sqrt{3} + 1)}{(\sqrt{3} - 1)(\sqrt{3} + 1)} \\ &= \frac{1.6(\sqrt{3} + 1)}{(\sqrt{3})^2 - (1)^2} \\ &= \frac{1.6(\sqrt{3} + 1)}{2} = 0.8(\sqrt{3} + 1) \end{aligned}$$

Therefore, the height of the pedestal is $0.8(\sqrt{3} + 1)$ m.

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Q9 The angle of elevation of the top of a building from the foot of the tower is 30° and the angle of elevation of the top of the tower from the foot of the building is 60° . If the tower is 50 m high, find the height of the building.

Answer.



Let AB be the building and CD be the tower.

In $\triangle CDB_1$

$$\frac{CD}{BD} = \tan 60^\circ$$

$$\frac{50}{BD} = \sqrt{3}$$

$$BD = \frac{50}{\sqrt{3}}$$

In $\triangle ABD$,

$$\frac{AB}{BD} = \tan 30^\circ$$

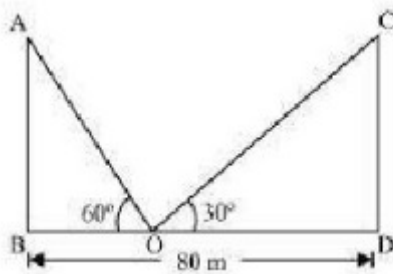
$$AB = \frac{50}{\sqrt{3}} \times \frac{1}{\sqrt{3}} = \frac{50}{3} = 16\frac{2}{3}$$

Therefore, the height of the building is $16\frac{2}{3}m$.

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Q10 Two poles of equal heights are standing opposite each other on either side of the road, which is 80 m wide. From a point between them on the road, the angles of elevation of the top of the poles are 60° and 30° , respectively. Find the height of poles and the distance of the point from the poles.

Answer.



Let AB and CD be the poles and O is the point from where the elevation angles are measured.

In $\triangle ABO$,

$$\frac{AB}{BO} = \tan 60^\circ$$

$$\frac{AB}{BO} = \sqrt{3}$$

$$BO = \frac{AB}{\sqrt{3}}$$

In $\triangle CDO$,

$$\frac{CD}{DO} = \tan 30^\circ$$

$$\frac{CD}{80-BO} = \frac{1}{\sqrt{3}}$$

$$CD\sqrt{3} = 80 - BO$$

$$CD\sqrt{3} = 80 - \frac{AB}{\sqrt{3}}$$

$$CD\sqrt{3} + \frac{AB}{\sqrt{3}} = 80$$

Since the poles are of equal heights,

$$CD = AB$$

$$CD \left[\sqrt{3} + \frac{1}{\sqrt{3}} \right] = 80$$

$$CD \left(\frac{3+1}{\sqrt{3}} \right) = 80$$

$$CD = 20\sqrt{3}\text{m}$$

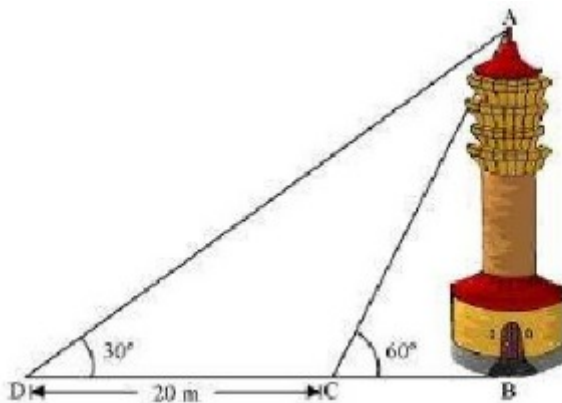
$$BO = \frac{AB}{\sqrt{3}} = \frac{CD}{\sqrt{3}} = \left(\frac{20\sqrt{3}}{\sqrt{3}} \right) \text{m} = 20\text{m}$$

$$DO = BD - BO = (80 - 20)\text{m} = 60\text{m}$$

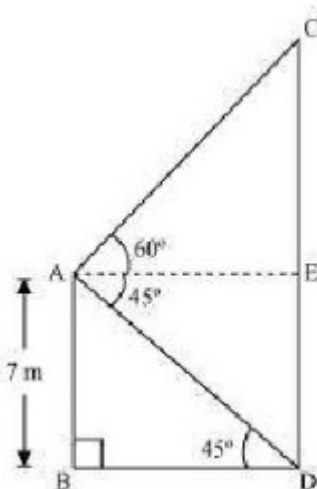
Therefore, the height of poles is $20\sqrt{3}$ m and the point is 20 m and 60 m far from these poles.

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Q11 A TV tower stands vertically on a bank of a canal. From a point on the other bank directly opposite the tower the angle of elevation of the top of the tower is 60° . From another point 20 m away from this point on the line joining this point to the foot of the tower, the angle of elevation of the top of the tower is 30° . Find the height of the tower and the width of the canal.



Answer.



Let AB be a building and CD be a cable tower.

In $\triangle ABD$,

$$\frac{AB}{BD} = \tan 45^\circ$$

$$\frac{7}{BD} = 1$$

$$BD = 7m$$

In $\triangle ACE$,

$$AC = BD = 7m$$

$$\frac{CE}{AE} = \tan 60^\circ$$

$$\frac{CE}{7} = \sqrt{3}$$

$$CE = 7\sqrt{3}m$$

$$CD = CE + ED = (7\sqrt{3} + 7)m$$

Therefore, the height of the cable tower is $7(\sqrt{3} + 1)m$.

$$\frac{AB}{BC} = \tan 60^\circ$$

$$\frac{AB}{BC} = \sqrt{3}$$

$$BC = \frac{AB}{\sqrt{3}}$$

In $\triangle ABD$

$$\frac{AB}{BD} = \tan 30^\circ$$

$$\frac{AB}{BC+CD} = \frac{1}{\sqrt{3}}$$

$$\frac{AB}{\frac{AB}{\sqrt{3}} + 20} = \frac{1}{\sqrt{3}}$$

$$\frac{AB\sqrt{3}}{AB+20\sqrt{3}} = \frac{1}{\sqrt{3}}$$

$$3AB = AB + 20\sqrt{3}$$

$$2AB = 20\sqrt{3}$$

$$AB = 10\sqrt{3}m$$

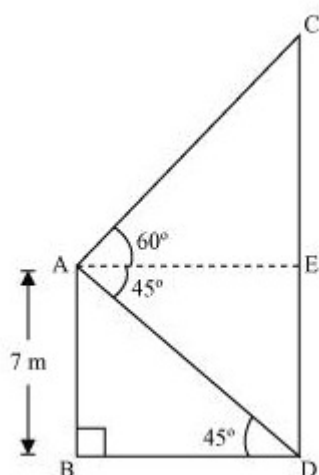
$$BC = \frac{AB}{\sqrt{3}} = \left(\frac{10\sqrt{3}}{\sqrt{3}}\right)m = 10m$$

Therefore, the height of the tower is $10\sqrt{3}m$ and the width of the canal is $10m$.

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Q12 From the top of a 7 m high building, the angle of elevation of the top of a cable tower is 60° and the angle of depression of its foot is 45° . Determine the height of the tower.

Answer.



Let AB be a building and CD be a cable tower.

In $\triangle ABD$,

$$\frac{AB}{BD} = \tan 45^\circ$$

$$\frac{7}{BD} = 1$$

$$BD = 7\text{m}$$

In $\triangle ACE$,

$$AE = BD = 7\text{ m}$$

$$\frac{CE}{AE} = \tan 60^\circ$$

$$\frac{CE}{7} = \sqrt{3}$$

$$CE = 7\sqrt{3}\text{m}$$

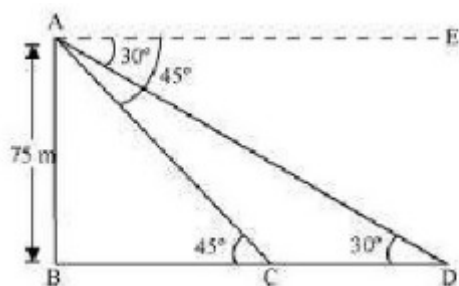
$$\begin{aligned} CD &= CE + ED = (7\sqrt{3} + 7)\text{m} \\ &= 7(\sqrt{3} + 1)\text{m} \end{aligned}$$

Therefore, the height of the cable tower is $7(\sqrt{3} + 1)\text{m}$

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Q13 As observed from the top of a 75 m high lighthouse from the sea-level, the angles of depression of two ships are 30° and 45° . If one ship is exactly behind the other on the same side of the lighthouse, find the distance between the two ships.

Answer.



Let AB be the lighthouse and the two ships be at point C and D respectively.

$$\frac{AB}{BC} = \tan 45^\circ$$

In triangle ABC, $\frac{75}{BC} = 1$

$$BC = 75\text{m}$$

In $\triangle ABD$,

$$\frac{AB}{BD} = \tan 30^\circ$$

$$\frac{75}{BC+CD} = \frac{1}{\sqrt{3}}$$

$$\frac{75}{75+CD} = \frac{1}{\sqrt{3}}$$

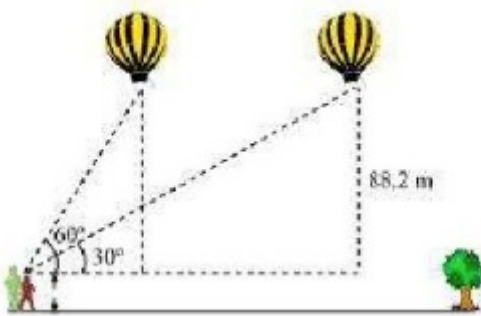
$$75\sqrt{3} = 75 + CD$$

$$75(\sqrt{3} - 1)\text{m} = CD$$

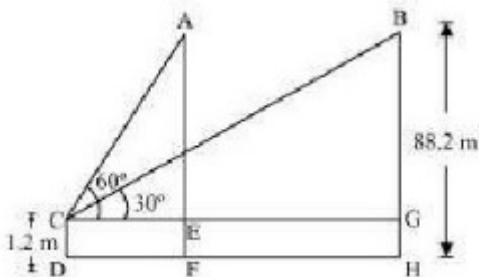
Therefore, the distance between the ships is $75(\sqrt{3} - 1)$ m.

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Q14 A 1.2 m tall girl spots a balloon moving with the wind in a horizontal line at a height of 88.2 m from the ground. The angle of elevation of the balloon from the eyes of the girl at any instant is 60° . After some the angle of elevation reduces to 30°



Answer.



Let the initial position A of balloon change to B after some time and CD be the girl. In $\triangle ACE$,

$$\frac{AE}{CE} = \tan 60^\circ$$

$$\frac{AF-EF}{CE} = \tan 60^\circ$$

$$\frac{88.2-1.2}{CE} = \sqrt{3}$$

$$\frac{87}{CE} = \sqrt{3}$$

$$CE = \frac{87}{\sqrt{3}} = 29\sqrt{3}\text{m}$$

In $\triangle BCG$,

$$\frac{BG}{CG} = \tan 30^\circ$$

$$\frac{88.2-1.2}{CG} = \frac{1}{\sqrt{3}}$$

Distance travelled by balloon = $EG = CG - CE$

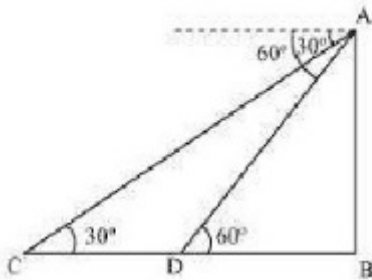
$$= (87\sqrt{3} - 29\sqrt{3})\text{m}$$

$$= 58\sqrt{3}\text{m}$$

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Q15 A straight highway leads to the foot of a tower. A man standing at the top of the tower observes a car as an angle of depression of 30° , which is approaching the foot of the tower with a uniform speed. Six seconds later, the angle of depression of the car is found to be 60° . Find the time taken by the car to reach the foot of the tower from this point.

Answer.



Let AB be the tower.

Initial position of the car is C, which changes to D after six seconds.

In $\triangle ADB$,

$$\frac{AB}{DB} = \tan 60^\circ$$

$$\frac{AB}{DB} = \sqrt{3}$$

$$DB = \frac{AB}{\sqrt{3}}$$

In $\triangle ABC$

$$\frac{AB}{BC} = \tan 30^\circ$$

$$\frac{AB}{BD+DC} = \frac{1}{\sqrt{3}}$$

$$AB\sqrt{3} = BD + DC$$

$$AB\sqrt{3} = \frac{AB}{\sqrt{3}} + DC$$

$$DC = AB\sqrt{3} - \frac{AB}{\sqrt{3}} = AB \left(\sqrt{3} - \frac{1}{\sqrt{3}} \right)$$

$$= \frac{2AB}{\sqrt{3}}$$

Time taken by the car to travel distance DC (i.e., $\frac{2AB}{\sqrt{3}}$) = 6 seconds

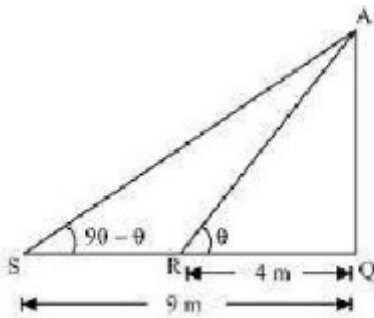
$$\text{Time taken by the car to travel distance DB (i.e., } \frac{AB}{\sqrt{3}}) = \frac{6}{\frac{2AB}{\sqrt{3}}} \times \frac{AB}{\sqrt{3}}$$

$$= \frac{6}{2} = 3 \text{ seconds}$$

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Q16 The angles of elevation of the top of a tower from two points at a distance of 4 m and 9 m, from the base of the tower and in the same straight line with it are complementary. Prove that the height of the tower is 6 m .

Answer.



Let AQ be the tower and R, S are the points 4 m, 9 m away from the base of the tower respectively.

The angles are complementary. Therefore, if one angle is θ , the other will be $90 - \theta$.

In $\triangle AQR$,

$$\frac{AQ}{QR} = \tan \theta$$

$$\frac{AQ}{4} = \tan \theta$$

In $\triangle AQS$,

$$\frac{AQ}{SQ} = \tan(90 - \theta)$$

$$\frac{AQ}{9} = \cot \theta$$

On multiplying equations (i) and (ii), we obtain

$$\left(\frac{AQ}{4} \right) \left(\frac{AQ}{9} \right) = (\tan \theta) \cdot (\cot \theta)$$

$$\frac{AQ^2}{36} = 1$$

$$AQ^2 = 36$$

$$AQ = \sqrt{36} = \pm 6$$

However, height cannot be negative.

Therefore, the height of the tower is 6 m.

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