NCERT SOLUTIONS CLASS - 8TH

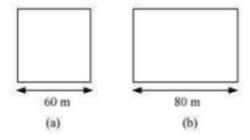




Class : 8th Subject : Maths Chapter : 11 Chapter Name : Mensuration

Exercise 11.1

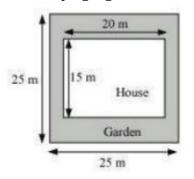
Q1 A square and a rectangular field with measurements as given in the figure have the same perimeter. Which field has a larger area?



Answer. Perimeter of square = 4 (Side of the square) = 4 (60 m) = 240 m. Perimeter of rectangle = 2 (Length + Breadth) = 2 (80 m + Breadth) = 160 m + 2 x Breadth It is given that the perimeter of the square and the rectangle are the same. 160 m + 2 x Breadth = 240 m Breadth of the rectangle = $\left(\frac{80}{2}\right)$ m = 40 m Area of square = (Side)² = (60m)² = 3600m² Area of rectangle = Length x Breadth = (80 x 40) m² = 3200 m² Thus, the area of the square field is larger than the area of the rectangular field.

Page: 171, Block Name: Exercise 11.1

Q2 Mrs. Kaushik has a square plot with the measurement as shown in the following figure. She wants to construct a house in the middle of the plot. A garden is developed around the house. Find the total cost of developing a garden around the house at the rate of ₹ 55 per m²

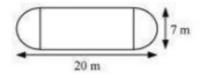


Answer. Area of the square plot = $(25m)^2 = 625m^2$

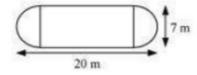
Area of the house = $(15 \text{ m}) \times (20 \text{ m}) = 300 \text{ }m^2$ Area of the remaining portion = Area of square plot - Area of the house = $625 \text{ }m^2 - 300 \text{ }m^2 = 325 \text{ }m^2$. The cost of developing the garden around the house is Rs 55 per m^2 . Total cost of developing the garden of area $325 \text{ }m^2 = \text{Rs} (55 \times 325)$ = Rs 17,875

Page: 171, Block Name: Exercise 11.1

Q3 The shape of a garden is rectangular in the middle and semi circular at the ends as shown in the diagram. Find the area and the perimeter of this garden [Length of rectangle is 20 - (3.5 + 3.5) metres].



Answer. Length of the rectangle = [20 - (3.5 + 3.5)] metres = 13 m Circumference of 1 semi-circular parts = nr = $\left(\frac{22}{7} \times 3.5\right)$ = 11 m Circumference of both semi-circular parts = (2×11) m = 22 m



Perimeter of the garden = AB + Length of both semi-circular regions BC and DA + CD = 13m + 22m + 13m = 48 m

Area of the garden = Area of rectangle + 2 x Area of two semi-circular regions = $\left[(13 \times 7) + 2 \times \frac{1}{2} \times \frac{22}{7} \times (3.5)^2 \right] m^2$ = $(91 + 38.5)m^2$ = $129.5m^2$

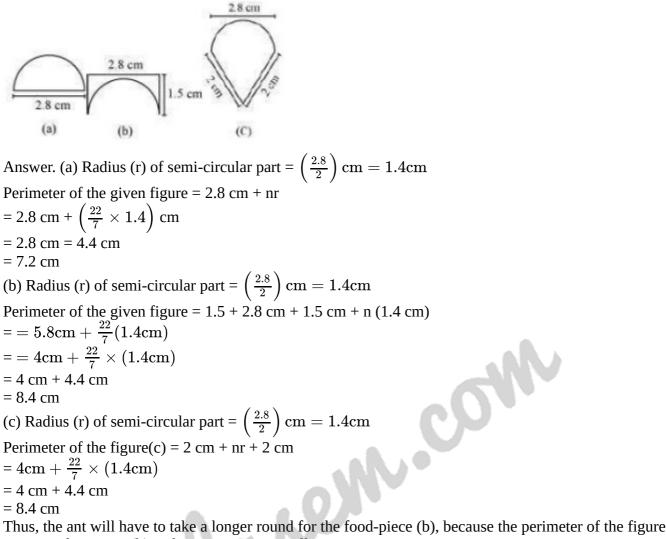
Page : 171 , Block Name : Exercise 11.1

Q4 A flooring tile has the shape of a parallelogram whose base is 24 cm and the corresponding height is 10 cm. How many such tiles are required to cover a floor of area 1080 m²? (If required you can split the tiles in whatever way you want to fill up the corners).

Answer. Area of parallelogram Base x Height Hence, area of one tile = 24 cm x 10 cm = 240 cm² Required number of tiles = $\frac{\text{Area of the floor}}{\text{Area of each tile}}$ = $\frac{1080\text{m}^2}{240\text{cm}^2} = \frac{(1080 \times 10000)\text{cm}^2}{240\text{cm}^2}$ (:: 1m = 100cm) = 45000 tiles Thus, 45000 tiles are required to cover a floor of area 1080 m².

Page : 171 , Block Name : Exercise 11.1

Q5 An ant is moving around a few food pieces of different shapes scattered on the floor. For which foodpiece would the ant have to take a longer round? Remember, circumference of a circle can be obtained by using the expression c = 2nr, where r is the radius of the circle.

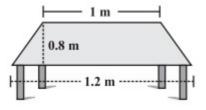


given in alternative (b) is the greatest among all.

Page : 171 , Block Name : Exercise 11.1

Exercise 11.2

Q1 The shape of the top surface of a table is a trapezium. Find its area if its parallel sides are 1 m and 1.2 m and perpendicular distance between them is 0.8 m.



Answer. Area of trapezium = $\frac{1}{2}$ (Sum of parallel sides) x (Distances between parallel sides) = $\left[\frac{1}{2}(1+1.2)(0.8)\right]$ m² = 0.88m²

Page : 177, Block Name : Exercise 11.2

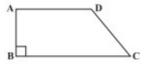
Q2 The area of a trapezium is 34 cm^2 and the length of one of the parallel sides is 10 cm and its height is 4 cm. Find the length of the other parallel side.

Answer. It is given that, area of trapezium = 34cm^2 and height = 4 cm Let the length of one parallel side be a. We know that, Area of trapezium = $\frac{1}{2}$ (Sum of parallel sides) x (Distances between parallel sides) $34\text{cm}^2 = \frac{1}{2}(10\text{cm} + a) \times (4\text{cm})$ 34 cm = 2(10 cm + a)17 cm = 10 cm + aa = 17 cm - 10 cm = 7 cm

Thus, the length of the other parallel side is 7 cm.

Page: 178, Block Name: Exercise 11.2

Q3 Length of the fence of a trapezium shaped field ABCD is 120 m. If BC = 48 m, CD = 17 m and AD = 40 m, find the area of this field. Side AB is perpendicular to the parallel sides AD and BC.

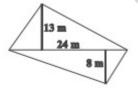


Answer. Length of the fence of trapezium ABCD = AB + BC + CD + DA 120 m = AB + 48 m + 17 m + 40m AB = 120 m - 105 m = 15 m Area of the field ABCD = $=\frac{1}{2}(AD + BC) \times AB$ $= \left[\frac{1}{2}(40 + 48) \times (15)\right] m^2$ $= \left(\frac{1}{2} \times 88 \times 15\right) m^2$

 $= 660 m^2$

Page : 178, Block Name : Exercise 11.2

Q4 The diagonal of a quadrilateral shaped field is 24 m and the perpendiculars dropped on it from the remaining opposite vertices are 8 m and 13 m. Find the area of the field.



Answer. It is given that, Length of the diagonal, d = 24 m Length of the perpendiculars, h_1 and h_2 , from the opposite vertices to the diagonal are h_1 = 8m and h_2 = 13 m Area of the quadrilateral = $=\frac{1}{2}d(h_1 + h_2)$ $=\frac{1}{2}(24m) \times (13m + 8cm)$ $=\frac{1}{2}(24m)(21m)$ $= 252m^2$ Thus, the area of the field is $252m^2$.

Page: 178, Block Name: Exercise 11.2

ow

Q5 The diagonals of a rhombus are 7.5 cm and 12 cm. Find its area.

Answer. Area of rhombus = $\frac{1}{2}$ (Product of its diagonals) Therefore, area of the given rhombus = $\frac{1}{2} \times 7.5$ cm $\times 12$ cm = 45cm²

Page : 178, Block Name : Exercise 11.2

Q6 Find the area of a rhombus whose side is 5 cm and whose altitude is 4.8 cm. If one of its diagonals is 8 cm long, find the length of the other diagonal.

Answer. Let the length of the other diagonal of the rhombus be x.

A rhombus is a special case of a parallelogram.

The area of a parallelogram is given by the product of its base and height.

Thus, area of the given rhombus = Base x Height = $6 \text{ cm x } 4 \text{ cm} = 24 \text{ cm}^2$

Also, area of rhombus = $\frac{1}{2}$ (Product of its diagonals)

$$egin{aligned} &\Rightarrow 24 \mathrm{cm}^2 = rac{1}{2}(8 \mathrm{cm} imes x) \ &\Rightarrow x = \left(rac{24 imes 2}{8}
ight) \mathrm{cm} = 6 \mathrm{cm} \end{aligned}$$

Thus, the length of the other diagonal of the rhombus is 6 cm.

Page : 178, Block Name : Exercise 11.2

Q7 The floor of a building consists of 3000 tiles which are rhombus shaped and each of its diagonals are 45 cm and 30 cm in length. Find the total cost of polishing the floor, if the cost per m^2 is \gtrless 4.

```
Answer. Area of rhombus = \frac{1}{2} (Product of diagonals)

Area of each tile

= \left(\frac{1}{2} \times 45 \times 30\right) cm<sup>2</sup>

= 675cm<sup>2</sup>

Area of 3000 tiles = (675 x 3000) cm<sup>2</sup> = 2025000 cm<sup>2</sup> = 202.5 m<sup>2</sup>

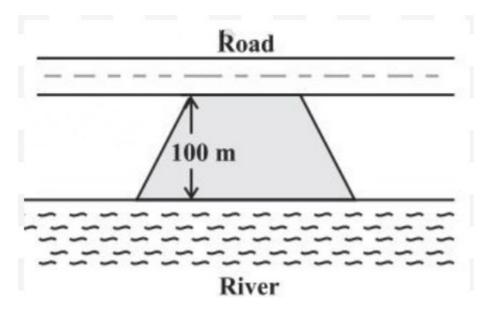
The cost of polishing is Rs 4 per m<sup>2</sup>.

Cost of polishing 202.5 m<sup>2</sup> area = Rs (4 x 202.5) = Rs 810

Thus, the cost of polishing the floor is Rs 810.
```

Page : 178, Block Name : Exercise 11.2

Q8 Mohan wants to buy a trapezium shaped field. Its side along the river is parallel to and twice the side along the road. If the area of this field is 10500 m^2 and the perpendicular distance between the two parallel sides is 100 m, find the length of the side along the river.



Answer. Let the length of the field along the road be I m. Hence, the length of the field along the river will be 2/ m.

Area of trapezium = $\frac{1}{2}$ (Sum of parallel sides) (Distance between the parallel sides)

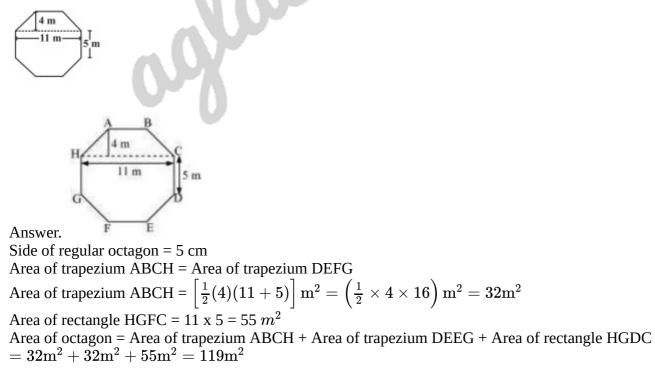
 $ightarrow 10500 \mathrm{m}^2 = rac{1}{2}(l+2l) imes (100 \mathrm{m})$

 $3l = \left(\frac{2 \times 10500}{100}\right) m = 210m$ l = 70 m

Thus, length of the field along the river = (2×70) m - 140 m

Page : 178 , Block Name : Exercise 11.2

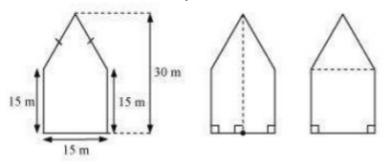
Q9 Top surface of a raised platform is in the shape of a regular octagon as shown in the figure. Find the area of the octagonal surface.



Page : 178, Block Name : Exercise 11.2

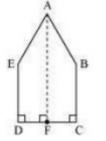
Q10 There is a pentagonal shaped park as shown in the figure. For finding its area Jyoti and Kavita

divided it in two different ways.



Find the area of this park using both ways. Can you suggest some other way of finding its area?

Answer. Jyoti's way of finding area is as follows.



Area of pentagon = 2 (Area of trapezium ABCF) $\left[2 imes rac{1}{2}(15+30)\left(rac{15}{2}
ight)
ight.$ m^2 = $337.5m^2$

Kavita's way of finding area is as follows.

Area of pentagon = Area of $\triangle ABE$ + Area of square BCDE $rac{1}{2} imes 15 imes (30-15)+(15)^2$ m^2 = $imes 15 imes 15 + 225
ight) {
m m}^2$ = $=(112.5+225){
m m}^2$ $= 337.5 m^2$

Page : 178, Block Name : Exercise 11.2

Q11 Diagram of the adjacent picture frame has outer dimensions = 24 cm × 28 cm and inner dimensions 16 cm \times 20 cm. Find the area of each section of the frame, if the width of each section is same.

븅 28 cm 2 16 cm 24 cm 28 cm ç 16 cm , cow M 24 cm Answer. Given that, the width of each section is same. Therefore, IB = BJ = CK = CL = DM = DN = AO = APIL = IB + 20 + CL28 = IB + 20 + CLIB + CL = 28 cm - 20 cm = 8 cmIB = CL = 4 cmHence, IB = BJ = CK = CL = DM = DN = AO = AP = 4cmArea of section BEFC = Area of section DGHA $=\left[rac{1}{2}(20+28)(4)
ight]\mathrm{cm}^2=96\mathrm{cm}^2$ Area of section ABEH = Area of section CDGF Page: 178, Block Name: Exercise 11.2

Q1 There are two cuboidal boxes as shown in the adjoining figure. Which box requires the lesser amount of material to make?

Answer. We know that, Total surface area of the cuboid = 2 (lh + bh + lb) Total surface area of the cube — $6(l)^2$ Total surface area of cuboid (a) = [2{(60) (40) + (40) (50) + (50) (60)}] cm² = [2(2400 + 2000 + 3000)] cm² = (2 x 7400) cm² = 14800 cm² Total surface area of cube (b) = 6 (50cm)² = 15000 cm². Thus, the cuboidal box (a) will require lesser amount of material.

Exercise 11.3

Page: 186, Block Name: Exercise 11.3

Q2 A suitcase with measures 80 cm \times 48 cm \times 24 cm is to be covered with a tarpaulin cloth. How many metres of tarpaulin of width 96 cm is required to cover 100 such suitcases?

Answer. Total surface area of suitcase = 2[(80)(48) + (48)(24) + (24)(80)]= 2[3840 + 1152 + 1920] $= 13824 \text{ cm}^2$ Total surface area of 100 suitcases = $(13824 \times 100) \text{ cm}^2 = 1382400 \text{ cm}^2$ Required tarpaulin = Length x Breadth 1382400 cm^2 = Length x 96 cm Length = $\left(\frac{1382400}{96}\right)$ cm = 14400 cm = 144 cm

Thus, 144 m of tarpaulin is required to cover 100 suitcases.

Page : 186, Block Name : Exercise 11.3

Q3 Find the side of a cube whose surface area is 600 cm^2 ?

```
Answer. Given that, surface area of cube = 600 \text{ cm}^2
Let the length of each side of cube be l.
Surface area of cube = 6( Side )^2
600 \text{cm}^2 = 6l^2
l^2 = 100 \text{cm}^2
L = 10 cm.
```

Page : 186, Block Name : Exercise 11.3

w.cow Q4 Rukhsar painted the outside of the cabinet of measure 1 m × 2 m × 1.5 m. How much surface area did she cover if she painted all except the bottom of the cabinet.

Answer. Length (1) of the cabinet = 2 mBreadth (b) of the cabinet = 1 mHeight (h) of the cabinet = 1.5 mArea of the cabinet that was painted = 2h(l+b) + lb $= [2 \times 1.5 \times (2 + 1) + (2) (1)] m^{2}$ $= [3(3) + 2] m^2$ $= (9+2) m^2$ $= 11 m^2$

Page : 186, Block Name : Exercise 11.3

Q5 Daniel is painting the walls and ceiling of a cuboidal hall with length, breadth and height of 15 m, 10 m and 7 m respectively. From each can of paint 100 m^2 of area is painted. How many cans of paint will she need to paint the room?

```
Answer. Given that,
Length (l) — 15 m, breadth (b) = 10 m, height (h) = 7 m
Area of the hall to be painted = Area of the wall + Area of the ceiling
= 2h(1+b) + 1b
= [2(7) (15 + 10) + 15 \times 10]m^2
= [14(25) + 150] m^2
= 500 \ m^2
It is given that 100 m^2 area can be painted from each can.
```

Number of cans required to paint an area of 500 m^2 . = 500/100 = 5Hence, 5 cans are required to paint the walls and the ceiling of the cuboidal hall.

Page : 186, Block Name : Exercise 11.3

Q6 Describe how the two figures at the right are alike and how they are different. Which box has larger lateral surface area?

Answer. Similarity between both the figures is that both have the same heights. The difference between the two figures is that one is a cylinder and the other is a cube. Lateral surface area of the cube = $4l^2 = 4(7 \text{ cm})^2 = 196 \text{ cm}^2$

Lateral surface area of the cylinder = $2rh = \left(2 \times \frac{22}{7} \times \frac{7}{2} \times 7\right)_{cm^2 = 154cm^2}$

Hence, the cube has larger lateral surface area.

Page : 186, Block Name : Exercise 11.3

Q7 A closed cylindrical tank of radius 7 m and height 3 m is made from a sheet of metal. How much sheet of metal is required?

Answer. Total surface area of cylinder = 2r (r+h)

$$= \left\lfloor 2 \times \frac{22}{7} \times 7(7+3) \right\rfloor_{\mathrm{m}^2}$$
$$= 440 \mathrm{m}^2$$

Thus, 440 m^2 sheet of metal is required.

Page : 186, Block Name : Exercise 11.3

Q8 The lateral surface area of a hollow cylinder is 4224 cm^2 . It is cut along its height and formed a rectangular sheet of width 33 cm. Find the perimeter of rectangular sheet?

Answer. A hollow cylinder is cut along its height to form a rectangular sheet. Area of cylinder = Area of rectangular sheet 4224cm² = 33 cm x Length Length = $\frac{4224 \text{cm}^2}{33 \text{cm}}$ = 128cm Thus, the length of the rectangular sheet is 128 cm. Perimeter of the rectangular sheet — 2 (Length + Width) = [2(128 + 33)] cm = (2 x 161) cm = 322 cm

Page : 186 , Block Name : Exercise 11.3

Q9 A road roller takes 750 complete revolutions to move once over to level a road. Find the area of the road if the diameter of a road roller is 84 cm and length is 1 m.

Answer. In one revolution, the roller will cover an area equal to its lateral surface area.

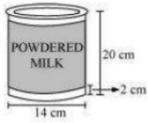
Thus, in 1 revolution, area of the road covered = 2rh $=2 imesrac{22}{7} imes42 ext{cm} imes1 ext{m}$ $=2 imes rac{22}{7} imes rac{42}{100}\mathrm{m} imes 1\mathrm{m}$ $=\frac{264}{100}$ m²

In 750 revolutions, area of the road covered

$$=\left(750 imesrac{264}{100}
ight)\mathrm{m}^2
onumber = 1980\mathrm{m}^2$$

Page : 186 , Block Name : Exercise 11.3

Q10 A company packages its milk powder in cylindrical container whose base has a diameter of 14 cm and height 20 cm. Company places a label around the surface of the container (as shown in the figure). If the label is placed 2 cm from top and bottom, what is the area of the label.



Answer. Height of the label = 20 cm - 2 cm - 2 cm = 16 cm Radius of the label = $\left(\frac{14}{2}\right)$ cm = 7 cm Label is in the form of a cylinder having its radius and height as 7 cm and 16 cm. Area of the label = 2 (Radius) (Height) = $\left(2 \times \frac{22}{7} \times 7 \times 16\right)$ cm² = 704 cm²

Page : 186 , Block Name : Exercise 11.3

Exercise 11.4

- Q1 Given a cylindrical tank, in which situation will you find surface area and in which situation volume.
- (a) To find how much it can hold.
- (b) Number of cement bags required to plaster it.
- (c) To find the number of smaller tanks that can be filled with water from it.

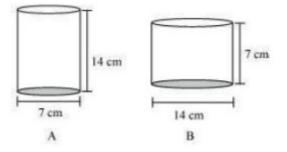
Answer. (a) In this situation, we will find the volume.

(b) In this situation, we will find the surface area.

(c) In this situation, we will find the volume.

Page : 191 , Block Name : Exercise 11.4

Q2 Diameter of cylinder A is 7 cm, and the height is 14 cm. Diameter of cylinder B is 14 cm and height is 7 cm. Without doing any calculations can you suggest whose volume is greater? Verify it by finding the volume of both the cylinders. Check whether the cylinder with greater volume also has greater surface area?



Answer. The heights and diameters of these cylinders A and 3 are interchanged.

We know that,

Volume of cylinder = $\pi r^2 h$ If measures of r and h are same, then the cylinder with greater radius will have greater area. Radius of cylinder A = $\frac{7}{2}$ cm Radius of cylinder B = $\left(\frac{14}{2}\right)_{cm} = 7cm$ As the radius of cylinder 3 is greater, therefore, the volume of cylinder 3 will be greater. Let us verify it by calculating the volume of both the cylinders. 2M°-CON Volume of cylinder A = $\pi r^2 h$ $=\left(rac{22}{7} imesrac{7}{2} imesrac{7}{2} imes14
ight)\mathrm{cm}^{3}$ $= 539 cm^{3}$ Volume of cylinder B = $\pi r^2 h$ $=\left(rac{22}{7} imes7 imes7 imes7
ight)\mathrm{cm}^{3}$ $=1078 \text{cm}^{3}$ Volume of cylinder B is greater. Surface area of cylinder $A = 2\pi r(r+h)$ $=\left[2 imesrac{22}{7} imesrac{7}{2}\Big(rac{7}{2}+14\Big)
ight]\mathrm{cm}^2$ $=\left[22 imes\left(rac{7+28}{2}
ight)
ight]\mathrm{cm}^{2}$ $=\left(22 imesrac{35}{2}
ight)\mathrm{cm}^2$ $= 385 \mathrm{cm}^2$ Surface area of cylinder B = $2\pi r(r + h)$ $=\left[2 imesrac{22}{7} imes7 imes(7+7)
ight]\mathrm{cm}^2$ $=(44 imes14)\mathrm{cm}^2$ $= 616 cm^{2}$ Thus, the surface area of cylinder a is also greater than the surface area of cylinder A.

Page : 191 , Block Name : Exercise 11.4

Q3 Find the height of a cuboid whose base area is 180 cm2 and volume is 900 cm3 ?

Answer. Base area of the cuboid = Length x Breadth = 180 cm^2 Volume of cuboid = Length x Breadth x Height 900 cm³ = 180 cm^2 x Height Height (900/180)cm = 5 cm Thus, the height of the cuboid is 5 cm.

Page : 191 , Block Name : Exercise 11.4

Q4 A cuboid is of dimensions 60 cm \times 54 cm \times 30 cm. How many small cubes with side 6 cm can be placed in the given cuboid?

Answer. Volume of cuboid = 60 cm x 54 cm x 30 cm = 97200 cm³ Side of the cube = 6 cm Volume of the cube = $(6)^3$ cm³ = 216 cm³ Required number of cubes = $\frac{\text{Volume of the cuboid}}{\text{Volume of the cube}}$ = $\frac{97200}{216} = 450$ Thus, 450 cubes can be placed in the given cuboid.

Page: 191, Block Name: Exercise 11.4

Q5 Find the height of the cylinder whose volume is 1.54 m^3 and diameter of the base is 140 cm ?

Answer. Diameter of the base = 140 cm Radius (r) of the base = $\left(\frac{140}{2}\right)$ cm = 70cm = $\frac{70}{100}$ m Volume of cylinder = $\pi r^2 h$ $1.54\text{m}^3 = \frac{22}{7} \times \frac{70}{100}$ m $\times \frac{70}{100}$ m $\times h$ $h = \left(\frac{1.54 \times 100}{22 \times 7}\right)$ m = 1m Thus, the height of the cylinder is 1 m.

Page : 191 , Block Name : Exercise 11.4

Q6 A milk tank is in the form of cylinder whose radius is 1.5 m and length is 7 m. Find the quantity of milk in litres that can be stored in the tank?

con

```
Answer. Radius of cylinder = 1.5 m

Length of cylinder = 7 m

Volume of cylinder = \pi r^2 h

= \left(\frac{22}{7} \times 1.5 \times 1.5 \times 7\right) m^3

= 49.5m<sup>3</sup>

1m<sup>3</sup> = 1000L

Required quantity = (49.5 x 1000) L 49500 L

Therefore, 49500 L of milk can be stored in the tank.
```

Page : 191 , Block Name : Exercise 11.4

Q7 If each edge of a cube is doubled,(i) how many times will its surface area increase?(ii) how many times will its volume increase?

Answer. (i) Let initially the edge of the cube be l. Initial surface area = $6l^2$ If each edge of the cube is doubled, then it becomes 2l. New surface area = $6(2t)^2 = 24l^2 = 4 \times 6l^2$ Clearly, the surface area will be increased by 4 times. (ii) Initial volume of the cube = l^3 When each edge of the cube is doubled, it becomes 2l. New volume $(2l)^3 = 8l^3 = 8 \times l^3$ Clearly, the volume of the cube will be increased by 8 times. Page : 191, Block Name : Exercise 11.4

Q8 Water is pouring into a cuboidal reservoir at the rate of 60 litres per minute. If the volume of reservoir is $108 m^3$, find the number of hours it will take to fill the reservoir.

Answer. Volume of cuboidal reservoir = 108 m^3 = (108 x 1000) L = 108000 L It is given that water is being poured at the rate of 60 L per minute. That is, (60 x 60) L = 3600 L per hour Required number of hours = $\frac{108000}{3600}$ = 30 hours Thus, it will take 30 hours to fill the reservoir.

Page: 192, Block Name: Exercise 11.4

agaan on one