

Q1. Express the following rational numbers as decimals:

(i) $\frac{42}{100}$

(ii) $\frac{327}{500}$

(iii) $\frac{15}{4}$

Solution:

(i) By long division method

$$\begin{array}{r} 100 \overline{) 42} \end{array} \quad (0.42)$$

$$\begin{array}{r} 400 \\ \hline \end{array}$$

$$\begin{array}{r} 200 \\ \hline \end{array}$$

$$\begin{array}{r} 200 \\ \hline \end{array}$$

$$\begin{array}{r} 0 \\ \hline \end{array}$$

Therefore, $\frac{42}{100} = 0.42$

(ii) By long division method

$$\begin{array}{r} 500 \overline{) 327.000} \end{array} \quad (0.654)$$

$$\begin{array}{r} 3000 \\ \hline \end{array}$$

$$\begin{array}{r} 2700 \\ \hline \end{array}$$

$$\begin{array}{r} 2500 \\ \hline \end{array}$$

$$\begin{array}{r} 2000 \\ \hline \end{array}$$

$$\begin{array}{r} 2000 \\ \hline \end{array}$$

$$\begin{array}{r} 0 \\ \hline \end{array}$$

Therefore, $\frac{327}{500} = 0.654$

(iii) By long division method

$$\begin{array}{r} 4 \overline{) 15.00} \end{array} \quad (3.75)$$

$$\begin{array}{r} 12 \\ \hline \end{array}$$

$$\begin{array}{r} 30 \\ \hline \end{array}$$

$$\begin{array}{r} 28 \\ \hline \end{array}$$

$$\begin{array}{r} 20 \\ \hline \end{array}$$

$$\begin{array}{r} 20 \\ \hline \end{array}$$

$$\begin{array}{r} 0 \\ \hline \end{array}$$

Therefore, $\frac{15}{4} = 3.75$

Q2. Express the following rational numbers as decimals:

(i) $\frac{2}{3}$

(ii) $-\frac{4}{9}$

(iii) $-\frac{2}{15}$

(iv) $-\frac{22}{13}$

(v) $\frac{437}{999}$

Solution:

(i) By long division method

$$\begin{array}{r} 3 \overline{) 2.0000} \quad (0.66 \\ 18 \end{array}$$

$$\begin{array}{r} 18 \\ \hline 20 \end{array}$$

$$\begin{array}{r} 18 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 18 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 18 \\ \hline 2 \end{array}$$

Therefore, $\frac{2}{3} = 0.66$

(ii) By long division method

$$\begin{array}{r} 9 \overline{) 4.000} \quad (0.444 \\ 3600 \end{array}$$

$$\begin{array}{r} 3600 \\ \hline 4000 \end{array}$$

$$\begin{array}{r} 3600 \\ \hline 4000 \end{array}$$

$$\begin{array}{r} 3600 \\ \hline 4000 \end{array}$$

$$\begin{array}{r} 3600 \\ \hline 4000 \end{array}$$

$$\begin{array}{r} 3600 \\ \hline 4000 \end{array}$$

$$\begin{array}{r} 3600 \\ \hline 4000 \end{array}$$

Therefore, $-\frac{4}{9} = -0.444$

(iii) By long division method

$$\begin{array}{r} 15 \overline{) 2.00} \quad (1.333 \\ 15 \end{array}$$

$$\begin{array}{r} 15 \\ \hline 50 \end{array}$$

$$\begin{array}{r} 50 \\ \hline 45 \end{array}$$

$$\begin{array}{r} 45 \\ \hline 50 \end{array}$$

$$\begin{array}{r} 50 \\ \hline 45 \end{array}$$

$$\begin{array}{r} 45 \\ \hline 50 \end{array}$$

50

45

5

Therefore, $\frac{2}{15} = -1.333$

(iv) By long division method

13) 22.000 (1.69230769

13

90

78

120

117

30

26

40

39

100

91

90

78

120

117

3

Therefore, $-\frac{22}{13} = -1.69230769$

(v) By long division method

999) 437.0000 (0.43743

3996

3740

2997

7430

6993

4370

$$\begin{array}{r}
 3996 \\
 \hline
 3740 \\
 2997 \\
 \hline
 743
 \end{array}$$

Therefore, $\frac{437}{999} = 0.43743$

Q3. Look at several examples of rational numbers in the form of

$\frac{p}{q}$ ($q \neq 0$), where p and q are integers with no

common factor other than 1 and having terminating decimal representations. Can you guess what property q must satisfy?

Solution:

A rational number $\frac{p}{q}$ is a terminating decimal

only, when prime factors of q are 2 and 5 only. Therefore,

$\frac{p}{q}$ is a terminating decimal only, when prime

factorization of q must have only powers of 2 or 5 or both.